

# Numerical approach for the modelling of an aquaculture net in current with the method of Smoothed Particle Hydrodynamics

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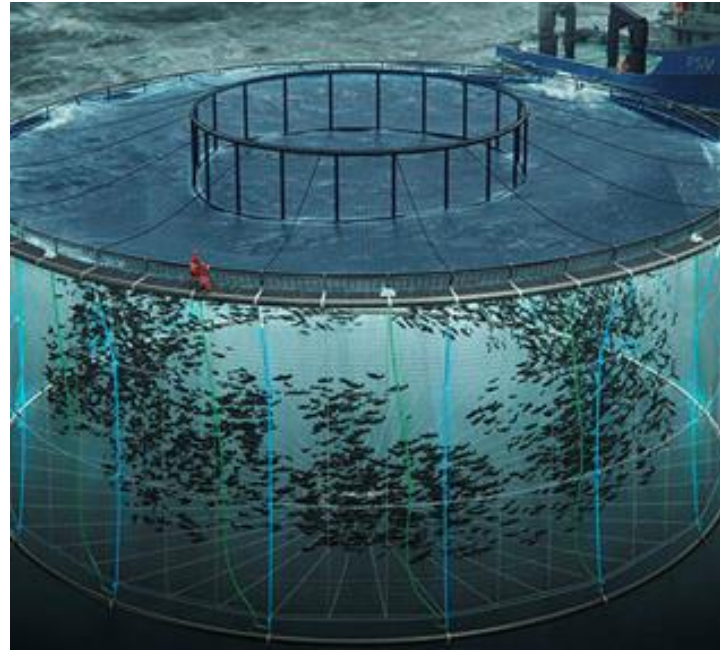
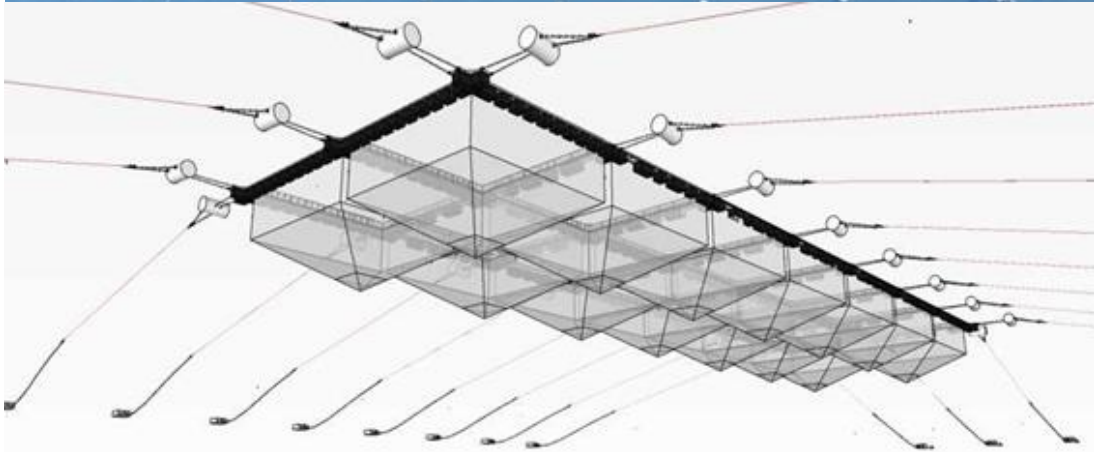
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Aquaculture net is one of the most important element in marine fish farming.



Environmental loads on the nets represent around 80% of the total loads on the fish cage.



Nylon nets



Copper alloy nets





## Traditional cage fish farming in Chile: Inshore areas



Marine fish aquaculture is traditionally done in areas protected from the direct action of the wind and waves.

### Design Parameters

Wave height ( $H_s$ ) < 3.5 m

Current velocity < 0.5 m/s

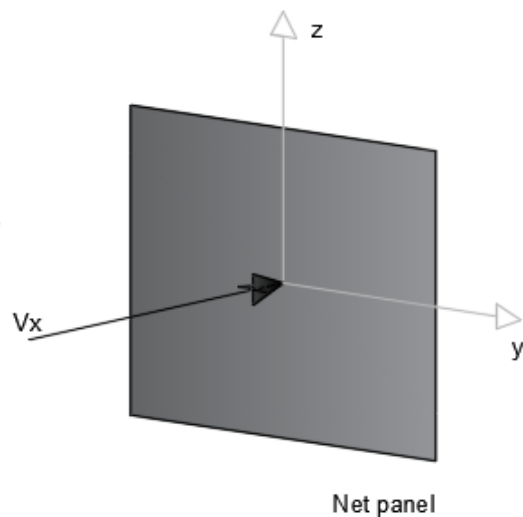
Wind velocity < 30 m/s

The methods developed to study the load on aquaculture net are based on:

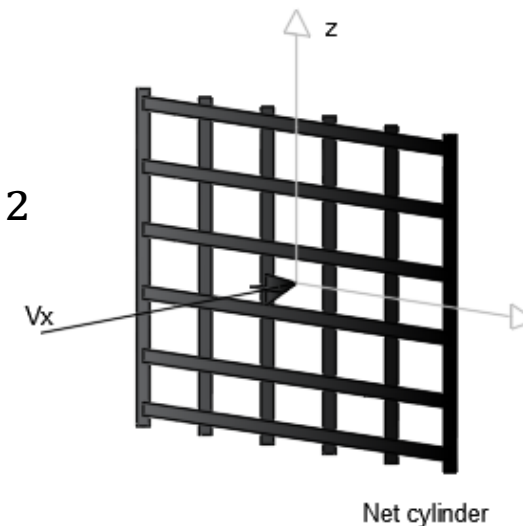
- a) Linear waves theory
- b) Morison equations

Where the net is modelled as a panel or a set of cylinders

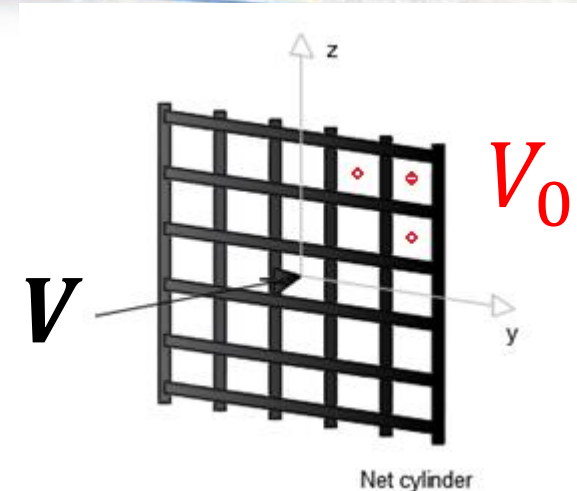
$$F_D = \frac{1}{2} \rho C_{net} A_t V^2$$



$$F_D = \frac{1}{2} \rho C_{net} d L_t V_0^2$$



When applying the cylinder array approach it's necessary to use the local velocity ( $V_0$ ) around the individual cylinder.



**Morison equation**

$$F_D = \frac{1}{2} \rho C_{cyl} d L_t V^2$$

**Set of cylinders**

$$F_D = \frac{1}{2} \rho C_{cyl} d L_t V_0^2$$

**Disturbed velocity**

$$V_0 = \frac{V}{1 - Sn}$$

Analytical drag coefficient

$$F_D = \frac{1}{2} \rho C_{cyl} \frac{1}{(1 - Sn)^2} d L_t V^2$$

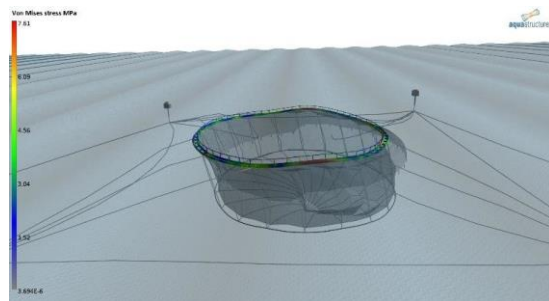
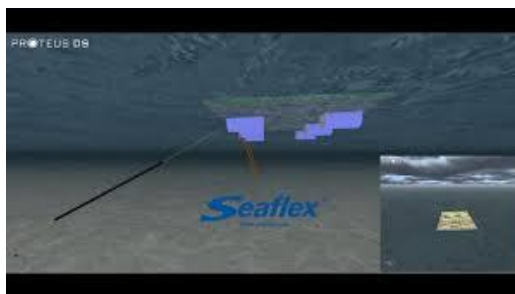
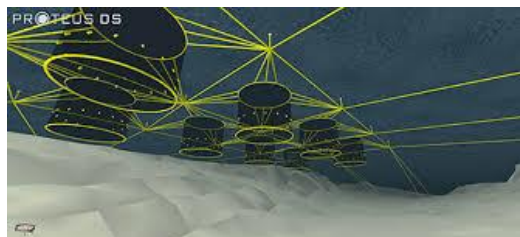
$$C_{net} = C_{d_{cyl}} \frac{1}{(1 - Sn)^2} \quad \text{Balash et al. (2009)}$$

$$C_{net} = C_{d_{cyl}} \frac{1}{\left(1 - \frac{Sn}{2}\right)^3} \quad \text{Berstad et al. (2012)}$$

$$C_{net} = C_{d_{cyl}} \frac{(2 - Sn)}{2(1 - Sn)^2} \quad \text{Kristiansen et al. (2012)}$$



These approaches are used by several commercial software:



These approaches have limitations:

- 1) There is not physical interaction between the net and the fluid.
- 2) The drag coefficient of the net is only defined by the solidity of the net and the drag coefficient of the cylinder

$$C_{net} = C_{d_{cyl}} \frac{1}{(1 - S_n)^2}$$

- 3) Parameters such as roughness, thread flexibility, and net material are not take into account.
- 4) The results are weakly consistent at velocities greater than 0.5 m/s (Cheng et al. 2020).



## Inshore Aquaculture

### Design Parameters

- Wave height ( $H_s$ )  $< 3.5$  m
- Current velocity  $< 0.5$  m/s
- Wind velocity  $\cong 30$  m/s



These methods are suitable for inshore aquaculture

## Exposed areas

### Design Parameters

- Wave height ( $H_s$ )  $> 3.5$  m
- Current velocity  $> 0.5$  m/s
- Wind velocity  $> 30$  m/s

## High-Energy Areas

- Large loads on the structure
- Important fluid-structure interaction (**nonlinear**)

Fish nets

- Large deformations
- Complex geometries

## Offshore Aquaculture

### Design Parameters

- Wave height ( $H_s$ )  $\cong 15$  m
- Current velocity  $\cong 1.5$  m/s
- Wind velocity  $\cong 40$  m/s



(North sea)

**SPH can be a solution**

# Numerical approach for the modelling of an aquaculture net with SPH



To model an aquaculture net, we need to take into account several hydrodynamic and structural parameters:

$$\frac{F_D}{\frac{1}{2} \rho V^2 d L} = C_D \left( \frac{V d}{\nu}, \frac{L_t d}{A_t}, \frac{K}{d}, k \frac{\Delta L}{T_i}, \dots \right)$$

Reynolds number ( $Re$ )

Solidity ( $Sn$ )

Relative roughness ( $e$ )

Stress and strain

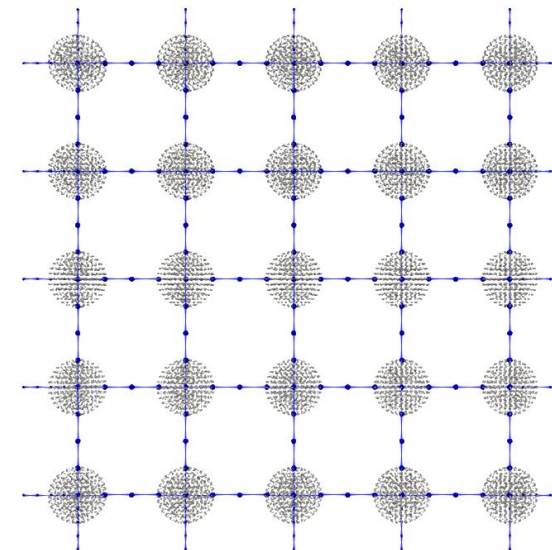


## Numerical Net

Using an SPH approach, we proposed to use the coupling between DualSPHysics and MoorDyn+

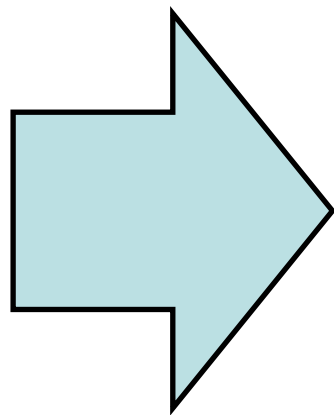


+



Where the net is modelled as a set of floating elements (spheres) and dynamic moorings.

# Input



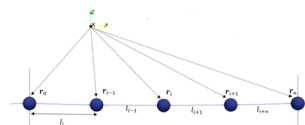
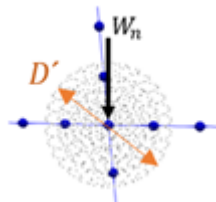
- Twine diameter
- Mesh size
- Net material

Solidity ( $S_n$ )

Density ( $\rho_M$ )  
Young`s modules (E)

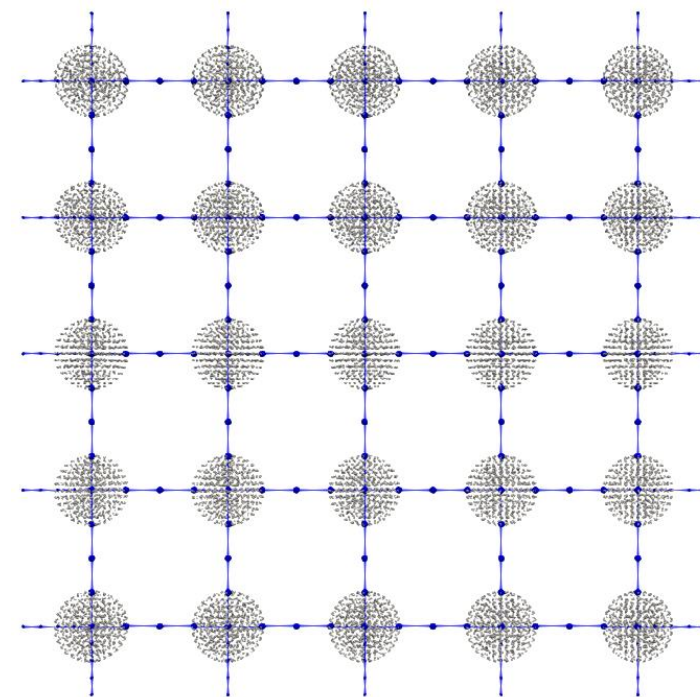
# Numerical Net

- Number ( $N$ )
- Density ( $\rho_{FE}$ )
- Diameter (D)
- Characteristics of connections



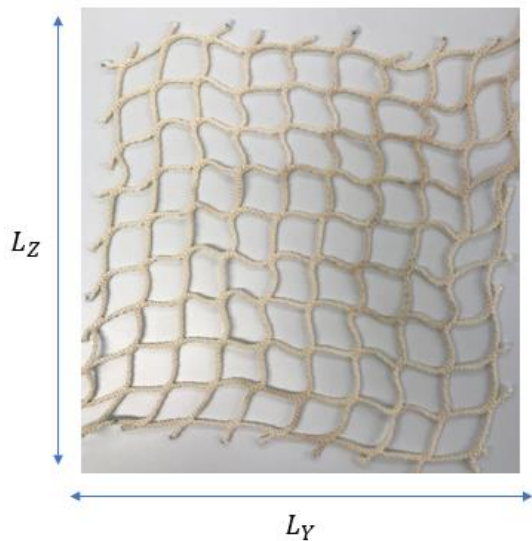
- Weight
- Diameter

# Output



$$Stiffness_{net} = Stiffness_{NM}$$

# Floating elements ( $D$ )



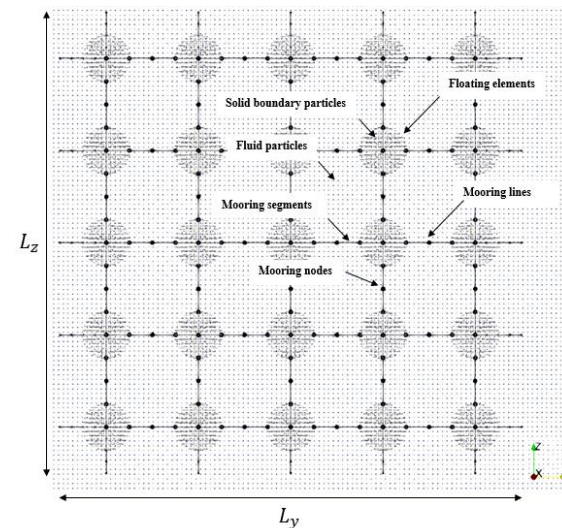
Solidity is a value of the net

$$S_n = \frac{A_e}{A_{tot}}$$

$$S_n = \frac{\text{Projected area of the twines}}{\text{Total area of the net}}$$

$$S_n = \frac{N * \left(\frac{\pi D^2}{4}\right)}{L_y L_z}$$

$$D = \sqrt{\frac{4 S_n L_y L_z}{N \pi}}$$



$$A_p = \frac{\pi D^2}{4}$$

$$S_n = \frac{N * \left(\frac{\pi D^2}{4}\right)}{L_y L_z}$$

This equation does not take into account the interaction between the net and the fluid



To overcome this, a corrected diameter ( $D'$ ) is established using an analytical approach.

$$Fd = N \frac{1}{2} \rho_w C_{sph} \frac{\pi D^2}{4} V_0^2$$



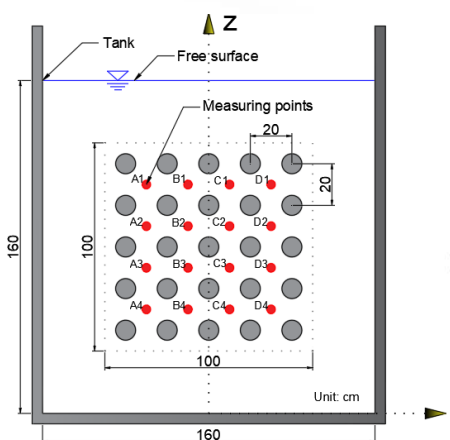
$$Fd = N \frac{1}{2} \rho_w C_{sph} \frac{\pi D^2}{4} \left( \frac{V}{1 - S_n} \right)^2$$



$$Fd = N \frac{1}{2} \rho_w C_{sph} \frac{\pi}{4} \frac{D^2}{(1 - S_n)^2} V^2$$

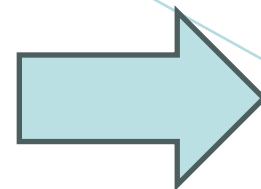
Disturbed velocity

$$V_0 = \frac{V}{1 - S_n}$$



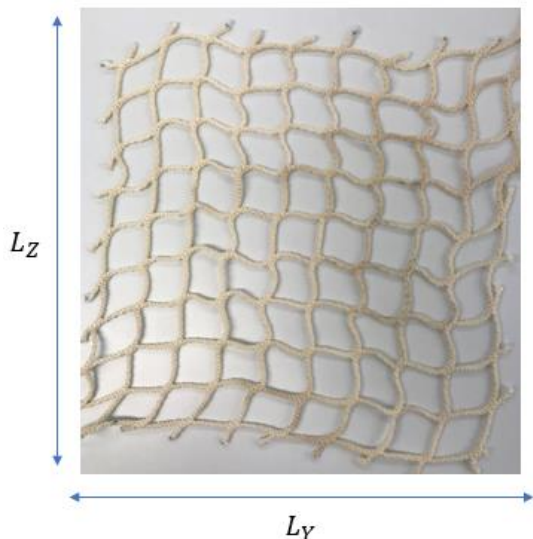
$$\beta = \frac{V}{V_0} + S_n$$

$$D' = \frac{D}{1 - S_n}$$



$$D' = \frac{D}{(\beta - S_n)}$$

# Characteristics of connections



$A_{net}$  = thread section area

$E_{net}$  = Young's Modules

$(N_y + N_z)_{net}$  = threads number

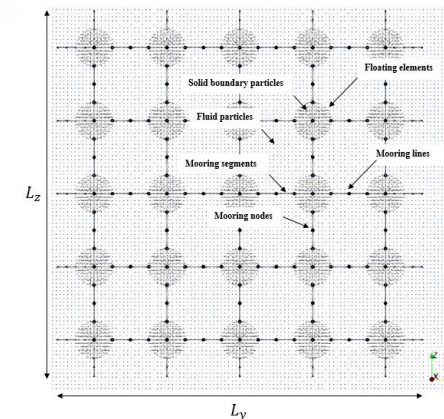
$$A_{net} E_{net} (N_y + N_z)_{net} \cong A_{NM} E_{NM} (N_Y + N_Z)_{NM}$$

$$\frac{A_{net} \cancel{E_{net}} (N_y + N_z)_{net}}{\cancel{E_{NM}} (N_Y + N_Z)_{NM}} \cong A_{NM}$$

$$E_{NM} = E_{net}$$

$$\frac{d_{net} (N_y + N_z)_{net}}{(N_Y + N_Z)_{NM}} \cong d_{NM}$$

(diameter)

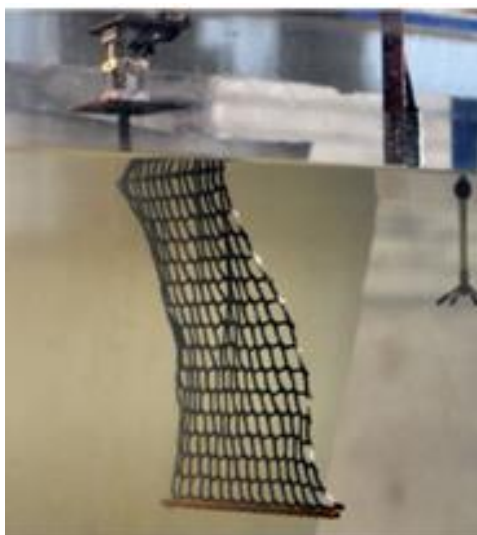


$$\rho_{FE} = 1000 \frac{kg}{m^3}$$

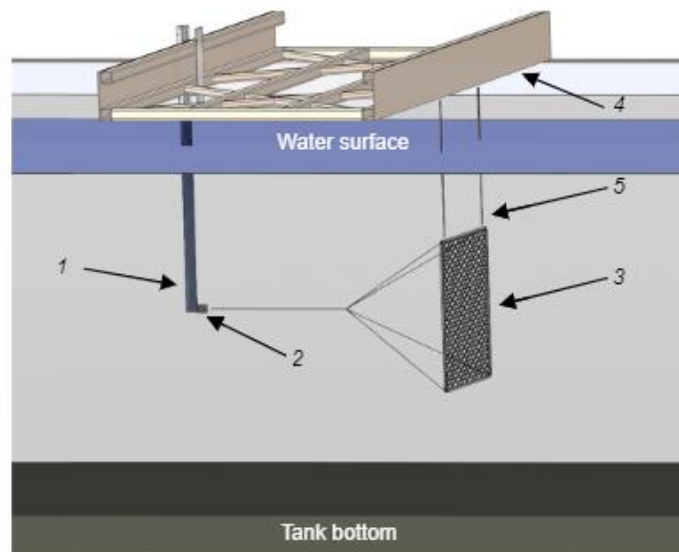
$$W_{net} \cong \sum W_{N_{ij}} + \sum W_i$$

(Weight)

# Validation cases



Physical Test (Bi *et al.* 2014)



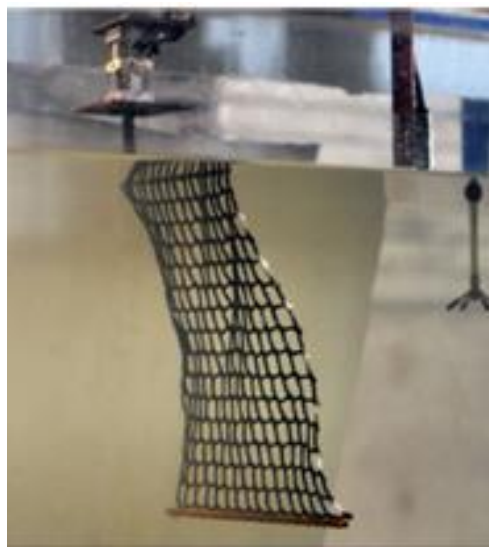
Physical Test (Tsukrov *et al.* 2011)



Physical Test (Cha and Lee, 2018)



# 1) Flat flexible net of polyethylene net in current



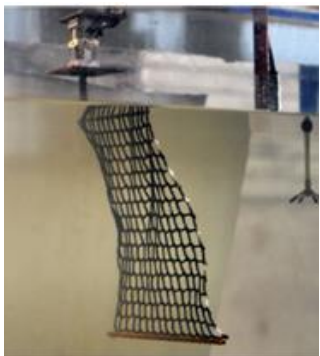
## Physical Test (Bi *et al.* 2014)

Size = 0.30 [m] x 0.30 [m]

$S_n = 0.26$

Material PE = 950 [ $kg/m^3$ ]

### Physical Test (Bi *et al.* 2014)



Twine diameter = 2.6 [mm]

Mesh size = 20 [mm]

Material PE = 950 [ $kg/m^3$ ]

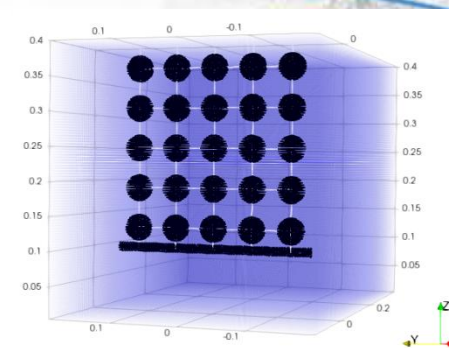
$S_n = 0.26$

Size = 0.30x0.30 [ $m^2$ ]

### Numerical Net

$N=25$        $m=0.126$  [kg/m]

$D'=4.35$  [cm]    $d=1.6$  [mm]

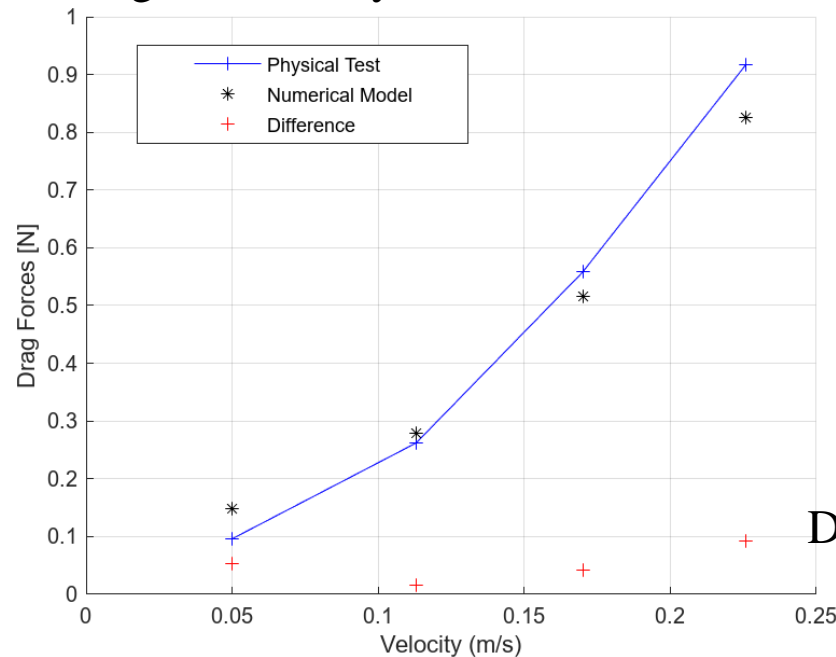


$\beta=1.06$

Resolution

$$dp = \frac{D'}{11}$$

### Drag Forces: Physical net v/s Numerical net



Difference

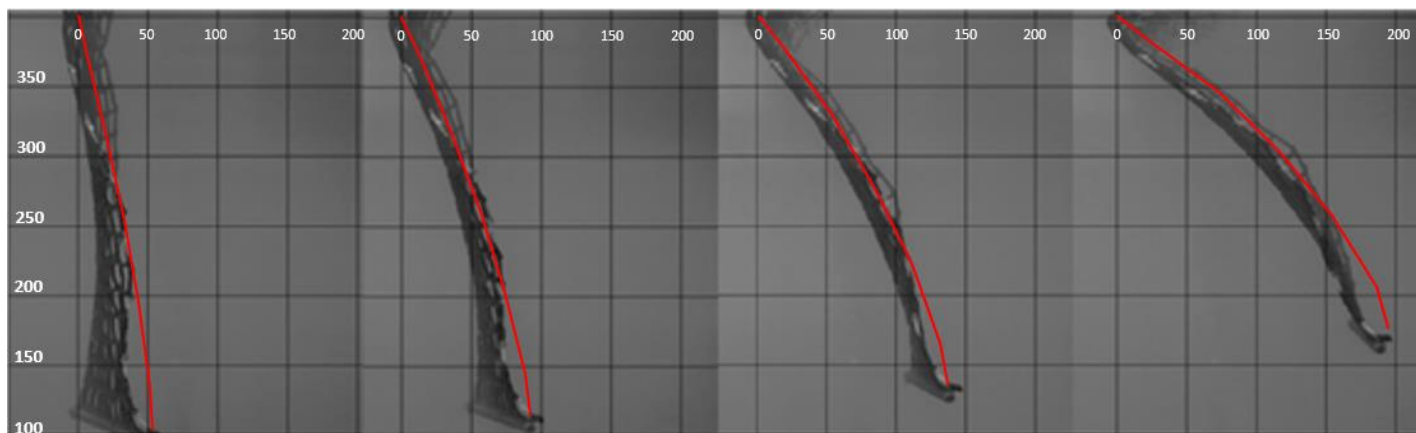
### Deformation: Physical net v/s Numerical net

$V = 0.058$  m/s

$V = 0.113$  m/s

$V = 0.170$  m/s

$V = 0.226$  m/s



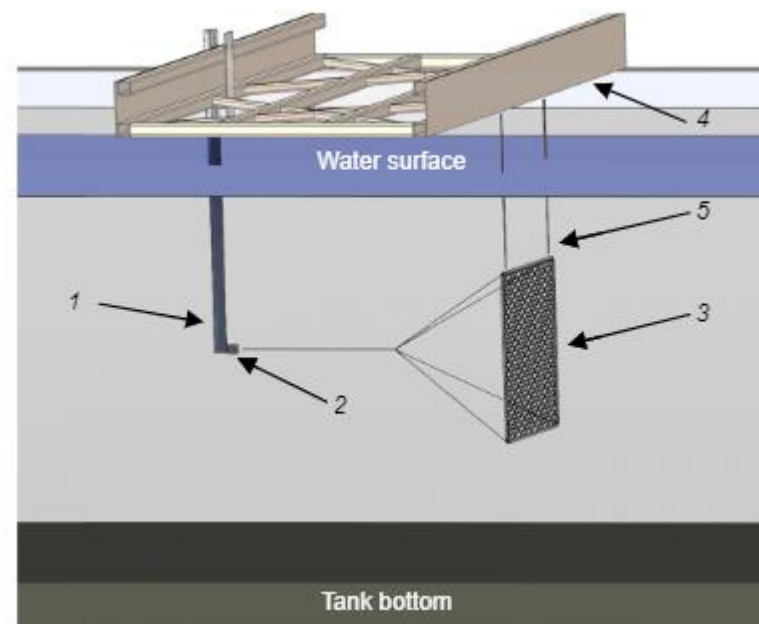
## 2) Flat copper alloy net in a rigid frame

### Physical Test (Tsukrov *et al.* 2011)

Size = 1.0 [m] x 1.0 [m]

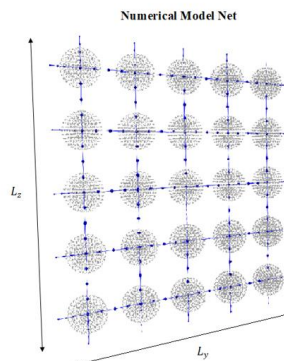
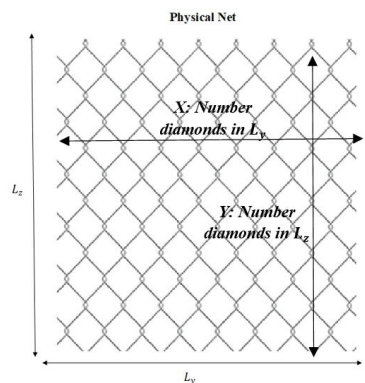
$S_n = 0.18$

Material UR = 8400 [ $kg/m^3$ ]





# Flat copper alloy net in a rigid frame in currents



## Physical Test

Size =  $1.0 \times 1.0$  [m<sup>2</sup>]

Twine diameter = 4 mm

Mesh size = 40 mm

Material UR = 8400 kg/m<sup>3</sup>

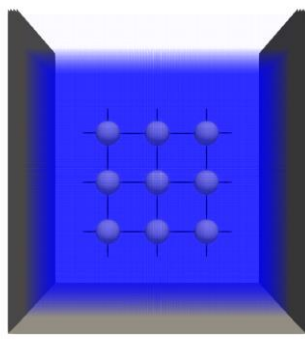
$S_n = 0.18$

N=9  $m=0.79$  [kg/m]

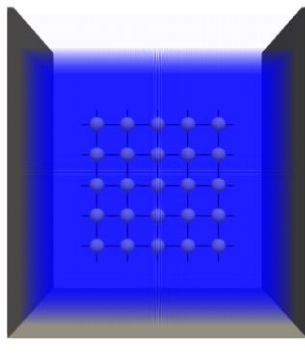
$D'=18.3$  [cm]  $d=1.06$  [cm]

N=25  $m=0.47$  [kg/m]

$D'=10.8$  [cm]  $d=0.83$  [cm]



$\beta=1.05$

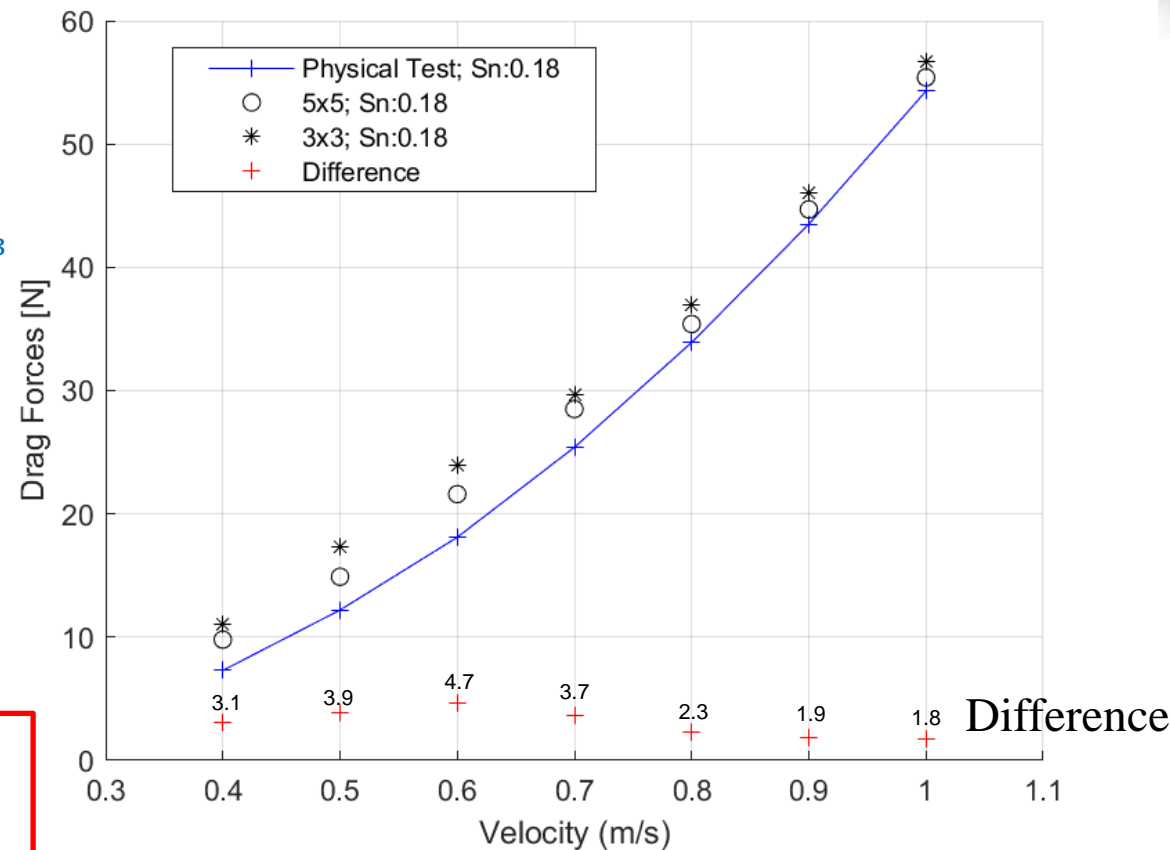


$\beta=1.07$

Resolution

$$dp = \frac{D'}{11}$$

## Drag Forces: Physical net v/s Numerical net



# 3) Floating fish cage (model) with copper alloy net in current

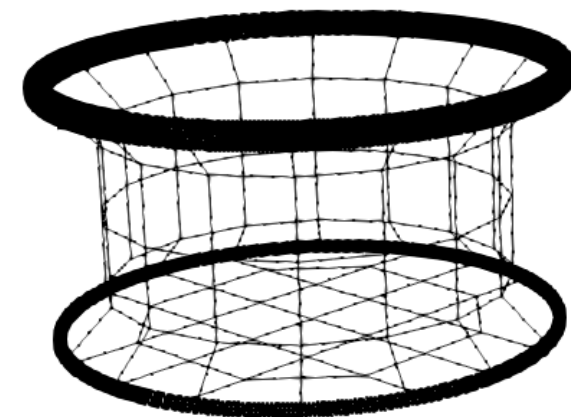
Physical test  
(Cha and Lee, 2018)



Fish Cage



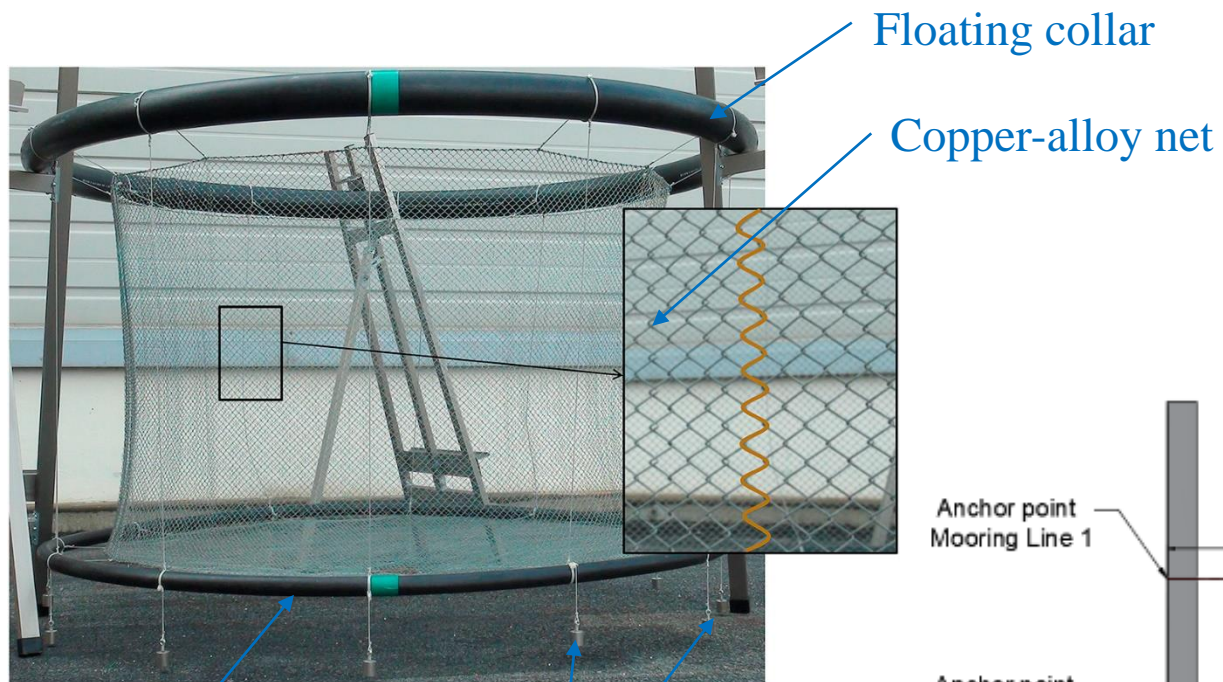
scale = 1/15



Numerical Model



## Physical fish cage (Cha and Lee, 2018)



Under water collar

Sinker

Resolution

$$dp = \frac{D'}{11}$$

## Numerical fish cage

Floating collar

Numerical net

$$N=69$$

$$d=0.033 \text{ [cm]}$$

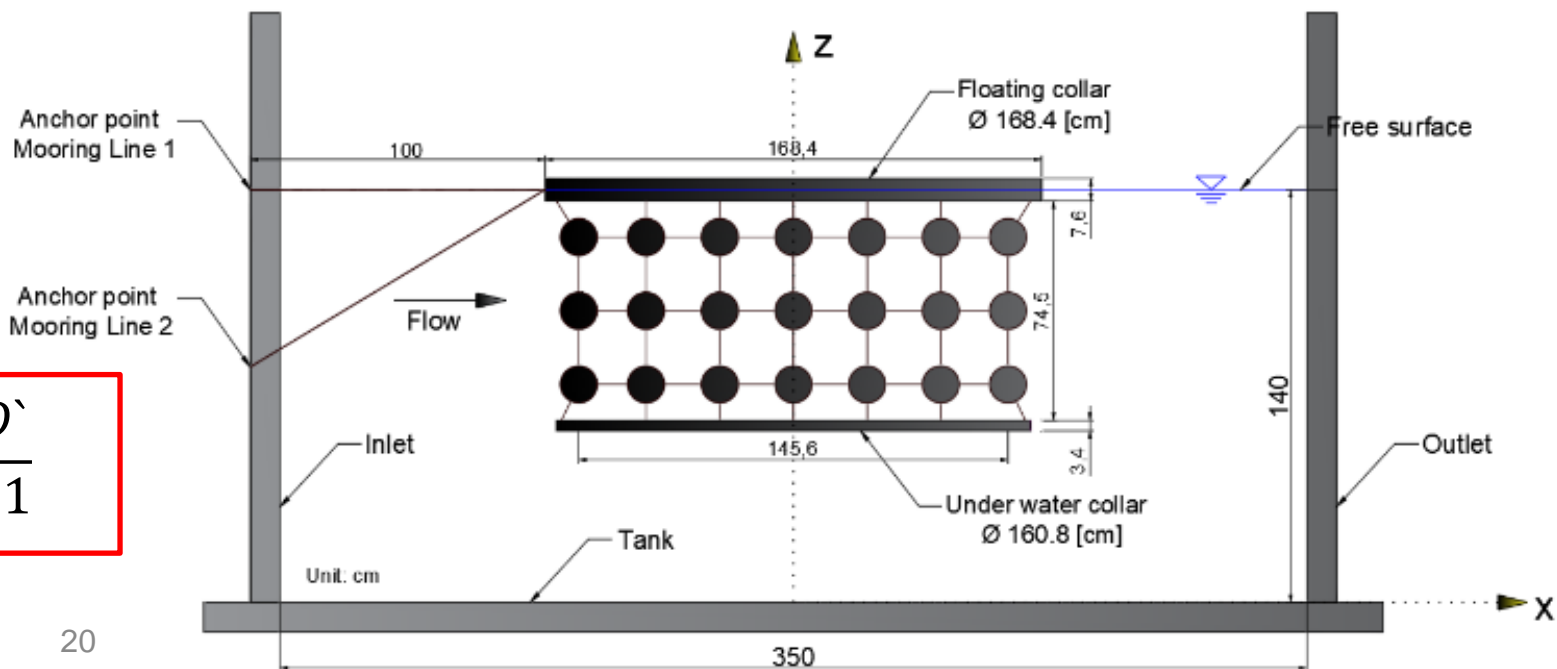
$$\beta=1.08$$

$$m=0.126 \text{ [kg/m]}$$

$$D'=12.98 \text{ [cm]}$$

$$E=10^{11} \text{ [Pa]}$$

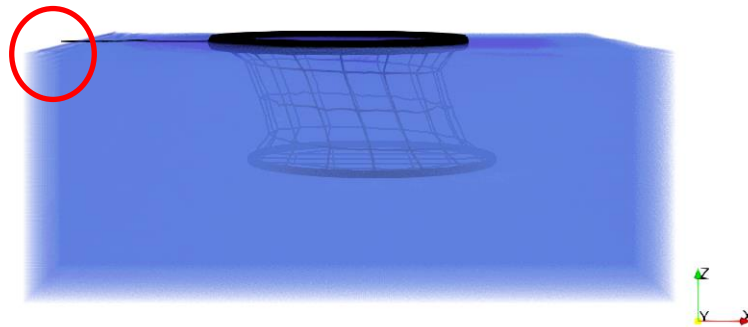
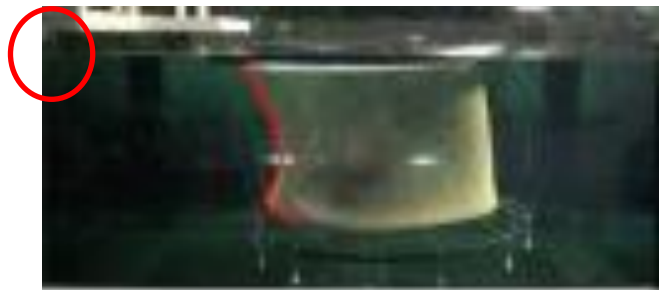
Under water collar (add sinker)



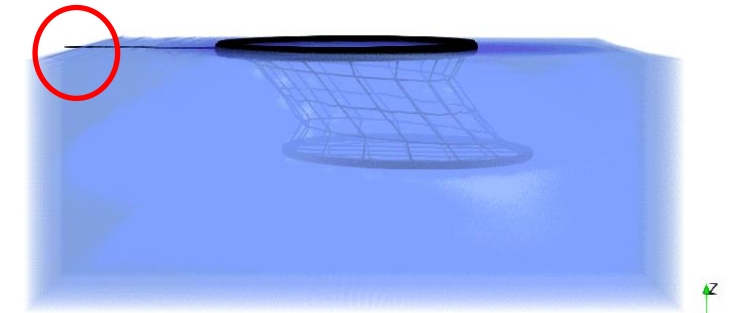


# 1) Loads on fish cage (Anchor point $z=0.0$ m)

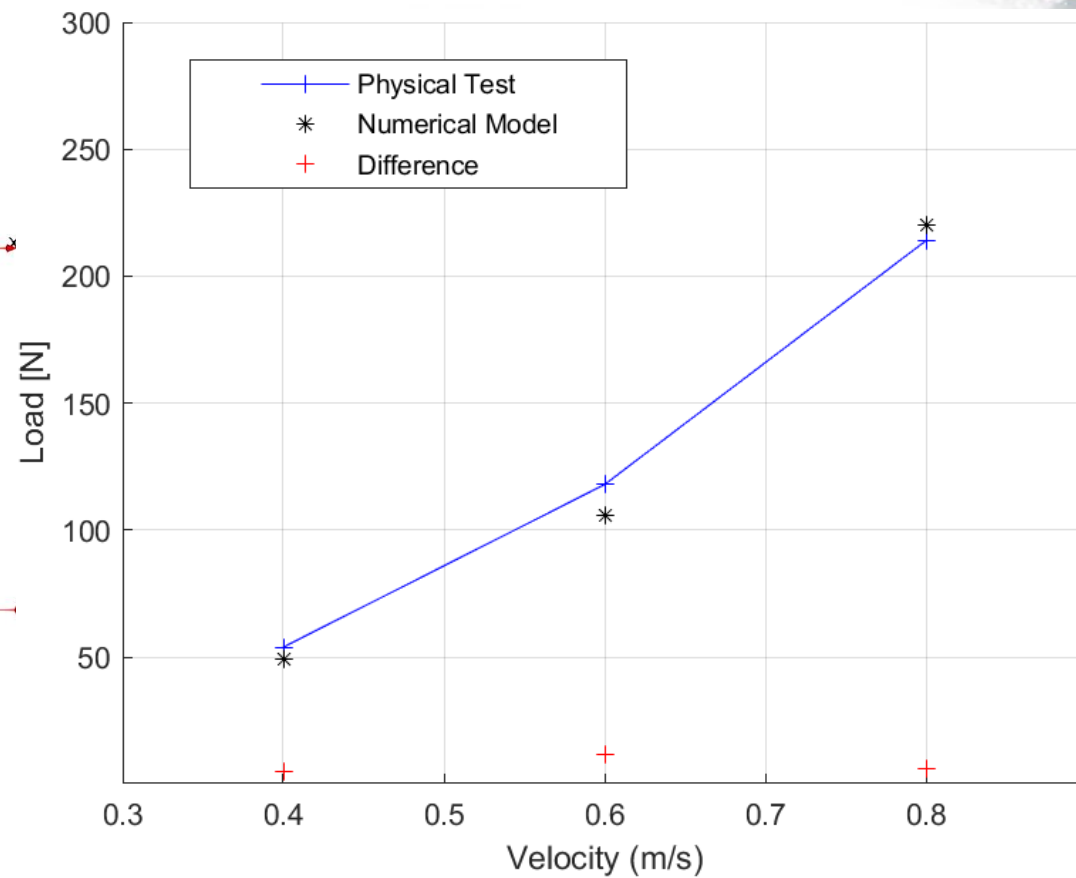
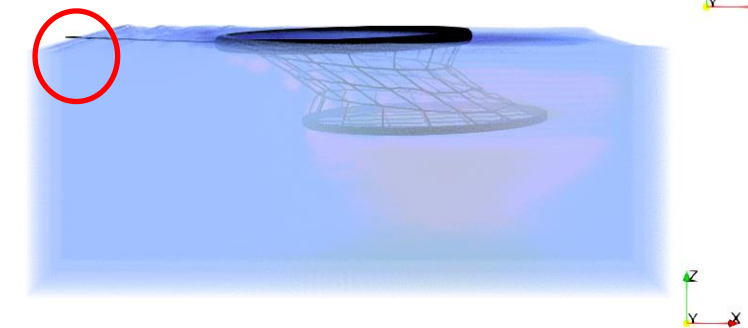
$V=0.4$  m/s



$V=0.6$  m/s



$V=0.8$  m/s



**V=0.4 m/s**



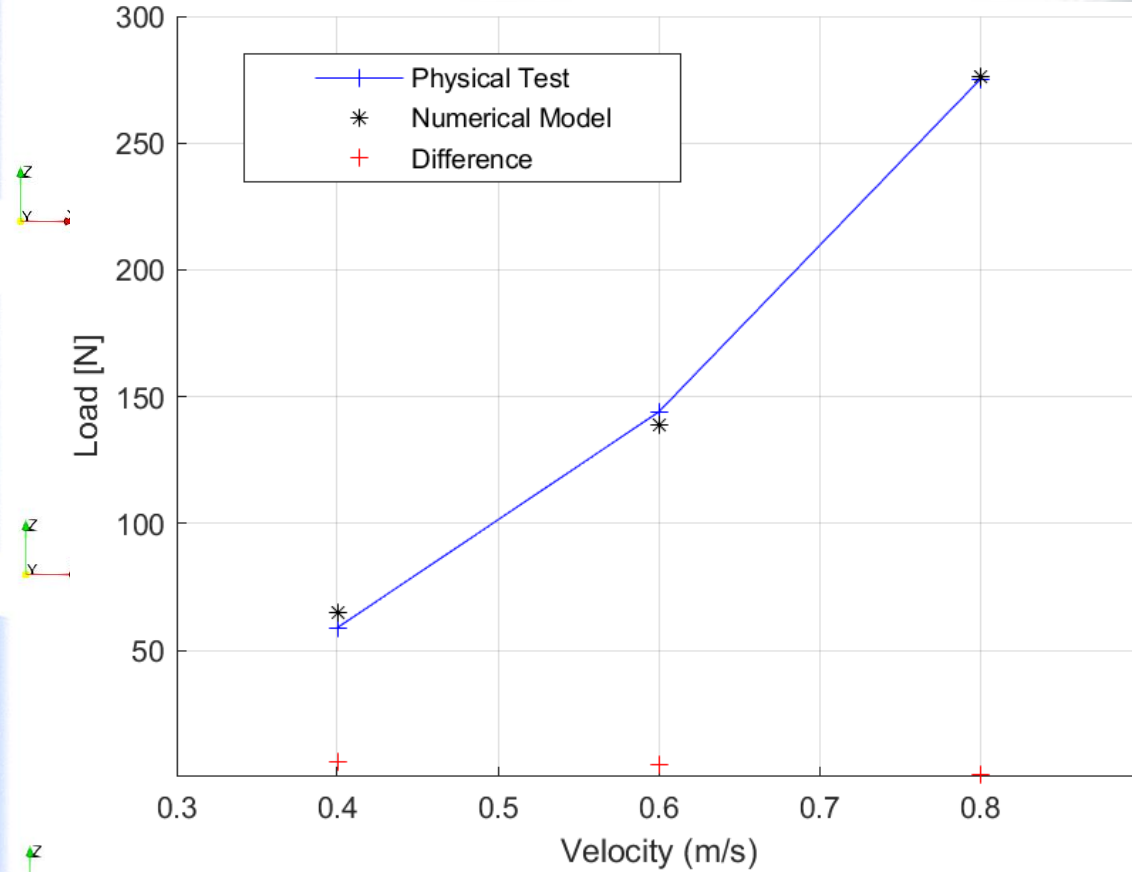
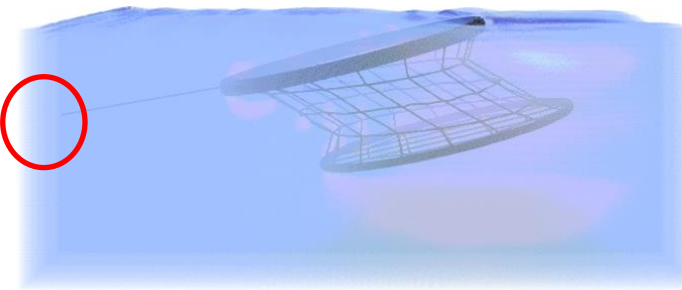
## 2) Loads on fish cage (Anchor point z= -0.6 m)



**V=0.6 m/s**



**V=0.8 m/s**



# Thank for you attention

